

Directions – Each problem below is arithmetic. Complete each one and show your work!

- 1.) What are the next four terms in the sequence
-
- 23, 28, 33,
- 38, 43, 48, 53
- , ...?

$$\begin{array}{r} \checkmark \quad \checkmark \\ 28-23 \quad 33-28 \\ =5 \quad =5 \end{array}$$

- 2.) What is the eighteenth term for the sequence
-
- 94, 106, 118, ...?

$$\begin{array}{r} \checkmark \quad \checkmark \\ 106-94 \quad 118-106 \\ =12 \quad =12 \end{array}$$

$$a_{18} = 94 + 12(18-1)$$

$$\boxed{a_{18} = 298}$$

- 3.) The thirty-fourth term of a sequence is -306 and the common difference is -8.

What is the second term of the sequence?

$$a_{34} = -306, d = -8 \rightarrow a_2 = ?$$

$$\begin{array}{l} \textcircled{1} -306 = a_1 - 8(34-1) \quad \textcircled{2} a_2 = -42 - 8 \\ -306 = a_1 - 264 \\ +264 \quad +264 \\ a_1 = -42 \end{array}$$

$$\boxed{a_2 = -50}$$

- 4.) What are the three arithmetic means for the sequence between 34 and 22?

$$34, \boxed{31, 28, 25}, 22$$

$$a_1, a_2, a_3, a_4, a_5$$

$$22 = 34 + d(5-1)$$

$$22 = 34 + 4d$$

$$-12 = 4d$$

$$d = -3$$

- 5.) The 23
- rd
- term of a sequence is 358 and the 15
- th
- term of the same sequence is 230.

What is the first term?

$$\begin{array}{l} a_{23} = 358 \quad \textcircled{1} 358 = a_1 + 22d \\ a_{15} = 230 \quad \textcircled{2} 230 = a_1 + 14d \end{array}$$

$$\begin{array}{l} \textcircled{2} 358 = a_1 + 22(16) \quad 128 = 8d \\ 358 = a_1 + 352 \quad d = 16 \\ \boxed{a_1 = 6} \end{array}$$

- 6.) What is the sum of the first six terms for the series of
- $a_n = 3n + 7$
- ?

$$a_1 = 3(1) + 7 = 10$$

$$a_2 = 3(2) + 7 = 13$$

$$a_3 = 3(3) + 7 = 16$$

$$a_4 = 3(4) + 7 = 19$$

$$a_5 = 3(5) + 7 = 22$$

$$a_6 = 3(6) + 7 = 25$$

$$\boxed{S_6 = 105}$$

- 7.) What is the sum of first 11 terms if the first term is 16 and the common difference is -4?

$$n = 11, a_1 = 16, d = -4 \rightarrow S_n = ?$$

$$\textcircled{1} a_{11} = 16 - 4(11-1)$$

$$a_{11} = -24$$

$$\textcircled{2} S_{11} = \frac{11}{2}(16 - 24)$$

$$\boxed{S_{11} = -44}$$

- 8.) What is the sum of the arithmetic series

$$25 + 39 + \dots + 179?$$

$$a_1 \checkmark 39-25 \Rightarrow d=14 \rightarrow a_n \rightarrow S_n = ?$$

$$\textcircled{1} 179 = 25 + 14(n-1) \quad \textcircled{2} S_{12} = \frac{12}{2}(25 + 179)$$

$$154 = 14n - 14$$

$$168 = 14n$$

$$n = 12$$

$$\boxed{S_{12} = 1224}$$

- 9.) The sum of first 23 terms is 3,496 and the first term is 9. What is the last term in the series?

$$S_{23} = 3496, a_1 = 9 \rightarrow a_n = ?$$

$$2 \cdot 3496 = \frac{23}{2}(9 + a_n) \cdot 2$$

$$6992 = 23(9 + a_n)$$

$$6992 = 207 + 23a_n$$

$$6785 = 23a_n \rightarrow \boxed{a_n = 295}$$

- 10.) What is the sum for
- $\sum_{n=3}^{10} (5n + 4)$
- linear eq.

$$n = 10 - 3 + 1 = 8$$

$$a_1 = 5(3) + 4 = 19$$

$$a_n = 5(10) + 4 = 54$$

$$S_8 = \frac{8}{2}(19 + 54)$$

$$\boxed{S_8 = 292}$$