

# Probability – Multiplying Probabilities

## Probability of Two Independent Events →

If two events, A and B, are independent (one event does not affect the next event),

then the probability of both events occurring is  $P(A \text{ and } B) = P(A) \cdot P(B)$

**Example 1:** Complete each problem about finding the probability of independent events.

<p>a.) At a picnic, Julio reaches into an ice-filled cooler containing 8 regular soft drinks and 5 diet soft drinks. He removes a can, then decides he is not really thirsty, and puts it back. Find the probability that Julio and the next person to reach into the cooler to get... <i>13 total drinks</i></p>			<p>b.) In a board game, three dice are rolled to determine the number of moves for the players. Find the probability of each given situation.</p> <p><i>Each of 3 die have #'s 1-6</i></p>		
<p>i.) Make a tree diagram of the situation stated above.</p>			<p>i.) <math>P(6, 6, 5)</math></p> $\frac{1}{6} \cdot \frac{1}{6} \cdot \frac{1}{6} = \frac{1}{216} = \boxed{.46\%}$	<p>v.) <math>P(\text{three } 5\text{'s})</math></p> $\frac{1}{6} \cdot \frac{1}{6} \cdot \frac{1}{6} = \frac{1}{216} = \boxed{.46\%}$	
			<p>ii.) <math>P(4, 4, \text{not } 4)</math></p> $\frac{1}{6} \cdot \frac{1}{6} \cdot \frac{5}{6} = \frac{5}{216} = \boxed{2.3\%}$	<p>vi.) <math>P(\text{any } \#, \text{ any } \#, \text{ not } 2)</math></p> $\frac{6}{6} \cdot \frac{6}{6} \cdot \frac{5}{6} = \frac{180}{216} = \boxed{83.3\%}$	
<p>ii.) <math>P(R, R)</math></p> $= \frac{8}{13} \cdot \frac{8}{13} = \frac{64}{169} = \boxed{37.9\%}$	<p>iii.) <math>P(D, R)</math></p> $= \frac{5}{13} \cdot \frac{8}{13} = \frac{40}{169} = \boxed{23.7\%}$	<p>iv.) <math>P(D, D)</math></p> $= \frac{5}{13} \cdot \frac{5}{13} = \frac{25}{169} = \boxed{14.8\%}$	<p>iii.) <math>P(\text{no } 3\text{'s})</math></p> $\frac{5}{6} \cdot \frac{5}{6} \cdot \frac{5}{6} = \frac{125}{216} = \boxed{57.9\%}$	<p>vii.) <math>P(1, 2, 3, \text{not } 4)</math></p> <p><i>4 dice → rolled 3 only</i></p> $\boxed{0\%}$	
			<p>iv.) <math>P(5, 6, 7)</math> <i>no 7 on die</i></p> $\frac{1}{6} \cdot \frac{1}{6} \cdot \frac{0}{6} = \frac{0}{216} = \boxed{0\%}$	<p>viii.) <math>P(\text{not } 3, \text{not } 4, 1)</math></p> $\frac{5}{6} \cdot \frac{5}{6} \cdot \frac{1}{6} = \frac{25}{216} = \boxed{11.6\%}$	

**Example 2:** You have a spinner that you will spin two times. Complete each problem.

<p>a.)</p>	<p>i.) Draw a diagram to show the probabilities.</p>	<p>b.)</p>	<p>i.) Draw a diagram to show the probabilities.</p>
<p>ii.) <math>P(\text{red}, \text{blue})</math></p> $\frac{1}{3} \cdot \frac{1}{3} = \frac{1}{9} = \boxed{11.1\%}$	<p>iii.) <math>P(\text{yellow}, \text{not red})</math></p> $\frac{1}{3} \cdot \frac{2}{3} = \frac{2}{9} = \boxed{22.2\%}$	<p>ii.) <math>P(\text{purple}, \text{yellow})</math></p> $\frac{1}{4} \cdot \frac{1}{4} = \frac{1}{16} = \boxed{6.25\%}$	<p>iii.) <math>P(\text{green}, \text{not purple})</math></p> $\frac{3}{4} \cdot \frac{3}{4} = \frac{9}{16} = \boxed{56.25\%}$



## Probability of Two Dependent Events →

If two events, A and B, are dependent (one event affects the next event),

then the probability of both events occurring is  $P(A \text{ and } B) = P(A) \cdot P(B \text{ following } A)$

**Example 3:** Complete each problem about finding the probability of dependent events.

a.) The host of a game show is drawing chips from a bag to determine the prizes for which contestants will play. Of the 10 chips in the bag, 6 show TELEVISION, 3 show VACATION, and 1 shows CAR. If the host draws the chips at random and does not replace them, then find each probability. <i>→ dependent</i>			b.) Three cards are drawn from a standard deck of cards without replacement. Find each probability. <i>→ dependent</i>	
i.) $P(V, \text{ then } C)$ $\frac{3}{10} \cdot \frac{1}{9}$ $= \frac{3}{90} = \frac{1}{30}$ $= .03 = \boxed{3.3\%}$	ii.) $P(T, \text{ then } T)$ $\frac{6}{10} \cdot \frac{5}{9}$ $= \frac{30}{90} = \frac{1}{3}$ $= .3 = \boxed{33.3\%}$	$P(C, \text{ then } A)$ $\frac{1}{10} \cdot \frac{0}{10}$ $= \frac{0}{10}$ $= \boxed{0\%}$	i.) $P(D, C, D)$ $\frac{13}{52} \cdot \frac{13}{51} \cdot \frac{12}{50}$ $= \frac{13}{850} = \boxed{1.5\%}$	ii.) $P(H, H, H)$ $\frac{13}{52} \cdot \frac{12}{51} \cdot \frac{11}{50}$ $= \frac{11}{850} = \boxed{1.3\%}$

**Example 4:** Determine whether the events are independent or dependent. Then find the probability.

- a.) Yana has 7 blue pens, 3 black pens, and 2 red pens in his desk drawer. *Total = 12 pens* If he selects three pens at random with no replacement, what is the probability that he will first select a blue pen, then a black pen, and then a red pen?  
*dependent (no replacement) →*  $P(\text{Blue, Black, Red}) = \frac{7}{12} \cdot \frac{3}{11} \cdot \frac{2}{10} = \frac{7}{220} = \boxed{3.2\%}$
- b.) A black die and a white die are rolled. What is the probability that a 3 shows on the black die and a 5 shows on the white die?  
*independent →*  $P(\text{black die 3 shows, white die 5 shows}) = \frac{1}{6} \cdot \frac{1}{6} = \frac{1}{36} = \boxed{2.8\%}$
- c.) Tami, Sonia, Michael, and Roger are the four candidates for student council president. If their names are placed in random order on the ballot, *Total* what is the probability that Michael's name will be first on the ballot followed by Sonia's name second?  
*dependent →*  $P(M, \text{ then } S) = \frac{1}{4} \cdot \frac{1}{3} = \frac{1}{12} = \boxed{8.3\%}$
- d.) Joe's wallet contains three \$1 bills, four \$5 bills, and two \$10 bills. If he selects three bills in succession, find the probability of selecting a \$10 bill, then a \$5 bill, and then a \$1 bill if the bills are not replaced.  
*9 bills total*  
*dependent →*  $P(\$10, \$5, \$1) = \frac{2}{9} \cdot \frac{4}{8} \cdot \frac{3}{7} = \frac{1}{21} = \boxed{4.8\%}$
- e.) A bag contains 6 green marbles and 8 yellow marbles. Carlos randomly selects one, puts it back, and then randomly selects another. What is the probability that Carlos selected one of each marble?  
*independent → 14 marbles total*  
 $P(1 \text{ green, } 1 \text{ yellow}) = \frac{6}{14} \cdot \frac{8}{14} = \frac{12}{49} = \boxed{24.5\%}$   
*independent*